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PLUNGING JET CHARACTERISTICS OF PLUNGING BREAKERS

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Abstract : With plunging breaking waves, air bubble entrainment is caused by the top of the wave forming a plunging jet and entraining air when it impacts the water in front of the wave. The potential for air bubble entrainment is related directly to the plunging jet impact characteristics. New experiments were performed in a two-dimensional wave flume. The breaking process was investigated with a high-speed video camera. The results provide new information on the breaking point characteristics, the jet impact conditions and the energy dissipation process. The entrainment of air bubbles is detailed. And the rate of energy dissipation by plunging breakers is estimated.

Key words : plunging breaking waves, plunging jet, energy dissipation, air entrainment, laboratory experiment.

Introduction

In lakes, estuaries and the ocean, gas transfer derives from free surface aeration. A substantial component of the mass transfer process occurs in the air bubble clouds entrained by breaking waves. The main mechanisms of air entrainment by breaking waves are spilling breakers and plunging breakers. In this study, only the plunging breaking wave type is examined as its potential for air bubble entrainment is much greater than the spilling wave type (COKELET 1977).

With plunging breakers, the entrainment of air bubbles is caused by the waves forming a water jet projecting ahead of the wave face and entraining air when it impacts the water free-surface in front of the wave (fig. 1). Several studies (e.g. KOGA 1982, HUBBARD et al. 1987) highlighted the lack of knowledge of the characteristics of plunging water jets in front of the breaking waves. The flow conditions at the impact of the water jet with the free-surface are most important in characterising the air bubble entrainment process. Recent reviews of air entrainment by plunging jets (e.g. BIN 1993, CHANSON 1995b) showed that the jet impact velocity V_i and the angle θ between the plunging jet and the free-surface of the receiving fluid are two dominant parameters for estimating the amount of entrained air and the sizes of entrained bubbles.

New experiments were performed in a wave flume. First the experimental apparatus is described. Then the characteristics of the plunging jet are described. The energy dissipation characteristics of plunging breakers are also discussed. Full details of the data and of experimental apparatus are reported in CHANSON and LEE (1995).

Experimental apparatus

New experiments were performed in a 10-m glass flume of uniform rectangular section. The channel width is $W = 0.3$ m and the sidewall height is 0.7 m. For all the experiments, the channel bed was horizontal and tap water was used.

One end of the flume is the wave generator which is controlled by a variable-speed electronic controller enabling a fine established-wave characteristic adjustment. The other end of the channel is a dissipation system (i.e. beach) consisting of inclined perforated steel plates, wave breaker models and plastic meshes. A sloping bottom was installed at 4.12 m downstream of the wave maker (fig. 2). The bottom slope was 4.8 degrees and the inclined bottom ended with a backward facing step. The geometry of this impervious sloping bottom and the deep-water wave characteristics were selected to induce breaking near the end of the sloping bottom with the plunging jet impacting downstream of the bottom edge in a region of large water depth. Further details on the channel characteristics were reported by LIN and HWUNG (1992) and HWUNG et al. (1992).

The water levels were measured with three wave gauges which were calibrated on-site with a graduated scale ($\Delta h < 0.5$ mm). The wave gauge resistances were scanned simultaneously at 100 Hz by a computer-controlled data acquisition system. For all the experiments, the deep-water wave characteristics were taken as that measured at the wave gauge No. 2. The error on the wave amplitude is estimated as $\Delta A < 0.5$ mm.

The wave breaking process was observed with a digital video-camera Sony™ CCD XC77RR using a one-millisecond shutter speed. The images were recorded on a video-recorder JVC™ HR-S5500V at a rate of 30 frames per second. Two camera positions were used : one at the end of the sloping bottom to investigate the wave breaking, and the other in front of the water pool to record the plunging jet impact. The camera was focused on the channel centreline and covered a window of about 0.45-m by 0.34-m.

Preparation of the experimental flow conditions

The same procedure was applied to each experiment (table 1). The water in the flume being perfectly still, the wave gauge data acquisition system and the video-recorder were started before the wave-maker. Because of the inertia of the wave maker, the first and second waves were not fully-developed and no breaking was observed. After several waves (i.e. usually after the 7th wave), two secondary effects were observed : a "backwashing" effect (i.e. flow returning effect), and some wave reflection effects.

The first effect is caused by an increase of volume of water at the end of the channel (i.e. downstream of the step). As a result wave breaking no longer occurred at the end of the sloping bottom. A similar backwashing effect was observed previously by other researchers (e.g. IVERSEN 1952). The second effect was caused by wave reflection from the beach at the downstream end of the channel. The wave reflections could induce small perturbations (i.e. wavelets) at the free-surface and the presence of wavelets perturbed the incoming waves and the video signal.

To avoid these effects, it was decided to investigate only the waves No. 3 to 7 for each run. Although the waves No. 3, 4 and 5 were sometimes undeveloped, their characteristics were close to those of fully-developed breaking waves. In each case the individual wave properties (as recorded with the wave gauges) were used as the incoming wave characteristics.

Experimental results

The wave characteristics at breaking and at the jet impact (definition in figure 2) were investigated for three still water levels (table 1). For each wave, the individual wave characteristics (wave celerity C_0 , wave amplitude A_0 , wave length L_0 , wave period T) were deduced from the wave gauge recordings.

At breaking near the edge of the sloping bottom, the wave amplitude A_b (above SWL), the wave height H_b (measured from crest to trough) and the horizontal velocity of wave crest V_b were measured when the downstream face of the breaker became vertical. Results are presented in figure 3. On figure 3(A), the breaking wave height is compared with the deep-water breaking theory (Mitchell theory) and the solitary wave theory (IPPEN 1966). Figure 3(B) presents the dimensionless breaking wave velocity V_b/C_0 as a function of the dimensionless breaking wave amplitude A_b/h . The results suggests that the breaking velocity is of the same order of magnitude as the deep-water wave celerity. In average for all experiments : $V_b/C_0 = 1.04$. Details of the experimental results are summarised in table 2 and compared with other results.

Figures 4 and 5 summarise the jet impact conditions A_i , θ and α measured when the free-falling plunging jet first impacts the downstream water surface. On figure 4, the dimensionless impact height A_i/A_b is plotted as a function of the wave steepness ratio A_0/L_0 , A_i being the impact height above SWL at jet impact (fig. 1). The results can be grouped in three regions as a function of the still water depth. Typically the ratio A_i/A_b ranges from 0 to 0.45 : i.e., wave impact occurs always above the still water level (SWL). Note the important scatter of the data.

The data of the impact angle θ of the plunging jet are presented on figure 5(A). For all the experiments, the results are best correlated by :

$$\theta = 41.2 - 364.1 * \frac{A_0}{L_0} \quad (1)$$

where θ is in degrees. It is worth noting that the jet impact angle is about 31 degrees (mean value for all experiments) and that θ decreases slightly with increasing wave amplitude and wave steepness. The former result is consistent with a re-analysis of plunging breaker photographs (COLES 1967, MELVILLE and RAPP 1985, LONGUET-HIGGINS 1988) in which θ ranged between 15 and 45 degrees.

Figure 5(B) shows the slope of the free-surface at impact with the horizontal. The data exhibit a wide range of scatter : i.e., between 0 and 35 degrees. Such a scatter is consistent with the scatter of impact height data. Indeed the shape of the free-surface in front of the breaking point is such that the free-surface slope at impact is expected to decrease with decreasing impact height A_i (as defined on fig. 1). Overall the order of magnitude of free-surface slope data is consistent with the re-analysis of photographs (COLES 1967, MELVILLE and RAPP 1985, LONGUET-HIGGINS 1988).

Discussion

Impact flow conditions

After wave breaking, the plunging water jet is in free-falling motion before impacting on the free-surface (fig. 1). For a free-falling jet, the impact flow conditions V_i and the jet angle with the horizontal ($\alpha + \theta$) can be deduced from simple jet trajectory equations as functions of the breaking velocity V_b and free-falling height ($A_b - A_i$). It yields :

$$V_i = \sqrt{V_b^2 + 2 * g * (A_b - A_i)} \quad (2)$$

$$\tan(\alpha + \theta) = \frac{\sqrt{2 * g * (A_b - A_i)}}{V_b} \quad (3)$$

On figure 6, the measured jet angle with horizontal ($\alpha + \theta$) is compared with equation (3). The agreement between the data and a simple trajectory equation is fair although not excellent.

Bubble penetration depth

Following the impact of the plunging water jet, entrained bubbles are carried downwards by the jet motion before being trapped in surrounding vortical motion. Later the bubble path becomes driven by buoyancy and the air bubbles rise to the free-surface. The maximum bubble penetration depth was recorded during the experiments. Results are shown on figure 7 where $(D_p)_{\max}$ is the maximum penetration depth measured vertically from the impingement point.

The results suggest that the air bubbles are entrained down to 1.2 to 2 times the wave amplitude below the free-surface. Such results must be considered as a pessimistic estimate for deep water waves as the effects of the flume bottom might be substantial. With plunging water jets in shallow waters, the submerged jet flow is deflected by the bottom. The change of momentum direction is accompanied by a local increase of pressure and of pressure gradient. The modification of the pressure field induces a modification of the bubble path as well as an increase of the buoyancy effects, the bubble rise velocity being proportional to the square root of the vertical pressure gradient.

Energy dissipation by plunging breaking waves

The energy dissipation by breaking waves can be estimated from the incident wave properties (H_I , T) and the wave transmission characteristics downstream of the breaking point. During the experiments, the incident flow properties were not available. Computations showed that the wave reflexion coefficient was not zero, implying that the measured wave height was in fact the superposition of the incident wave height and reflected wave height at that location.

The rate of energy dissipation by plunging breaking waves was deduced from the difference of the wave transmission energy for ideal fluid flow (BEM model) minus the measured wave transmission energy (data). The computations of the wave transmission energy with the BEM model provide the wave transmission energy in absence of wave breaking. Typical wave reflexion coefficients are reported in appendix A.

The potential flow computations were performed with a Boundary Element Method (BEM) model which was a simplification of that developed by LEE (1995) (see appendix A). The flow field was represented by 7 boundaries and 510 boundary elements. The incident wave flow conditions were set at the upstream open boundary. The computations provided the (ideal-flow) wave transmission downstream of the sloping bottom and the wave reflection caused by the sloping bottom.

During the experiments, the incident flow properties were not measured directly. They were estimated instead as the wave period T measured at wave gauge No. 2 and the measured wave height H_O at wave gauge No. 2.

Results are reported on figure 8. They show that the rate of energy dissipation ranges from 20% to 60% with a mean values of about 40%. Figure 8(B) suggests an increase of rate of energy dissipation with increasing bubble penetration depth which is best fitted by :

$$\frac{\Delta E}{E} = 31.2 * \left(\frac{(D_p)_{\max}}{A_0} \right)^{0.624} \quad (4)$$

After the impact of the free-falling jet with the free-surface, a turbulent shear flow develops below the free-surface. Kinetic energy is dissipated by turbulent shear in the shear layers. Additionally the transfer of momentum from the impinging flow to the surrounding fluid is dissipated by vortical and recirculatory flow motion. The bubble penetration depth gives some information on the shear flow characteristic length, and figure 8(B) shows an increase in energy dissipation with increasing shear flow length.

Comparison with energy dissipation by plunging jet at a drop structure

Energy dissipation by plunging jet is commonly used at drop structures and along stepped channels (e.g. fig. 9(A)). A simple analytical expression of the rate of energy dissipation by plunging jet can be developed :

$$\frac{\Delta E}{E} = 1 - \left(\frac{\frac{h}{h_c} + \frac{1}{2} * \left(\frac{h_c}{h} \right)^2}{\frac{3}{2} + \frac{\Delta z}{h_c}} \right) \quad (5)$$

$$\frac{h}{h_c} = \frac{2^{1/2}}{\frac{3}{2^{3/2}} + \sqrt{\frac{3}{2} + \frac{\Delta z}{h_c}}} \quad (6)$$

where h , h_c and Δz are defined on figure 9(A). Such calculations were successfully compared with a large number of experimental data (e.g. CHANSON 1995a).

For a plunging breaker the drop height equals $(A_b - A_i)$ (see fig. 1). At a drop structure, the critical flow depth is a characteristic jet thickness. For plunging breaking waves, CHANSON and CUMMINGS (1992) estimated a plunging jet thickness of about 0.01 to 0.1* H_b based upon a photographic analysis.

Assuming a plunging thickness of 0.1* H_b , the authors computed the equivalent rate of energy dissipation at drop structures for the wave flow conditions (see appendix A). The results (fig. 9(B)) indicate that the rate of energy dissipation by plunging jets is of the same magnitude for plunging breaking waves and at drop structures. The reasonably good agreement suggests some analogy in the mechanisms of energy dissipation.

It must be emphasised however that the analogy between drop structures and plunging breakers is limited by fundamental differences : drop structure flows are steady flows impacting into shallow waters while plunging breakers (as investigated in this study) are unsteady flows impacting in deeper waters.

Discussion

The energy dissipation calculations are based upon a number of approximations (denoted [H1] to [H5] below) that the authors wish to highlight.

The ideal fluid flow computations were performed for a steady flow [H1] and they are the solution of linear equations [H2]. The incident wave properties were taken as the measured wave height and period at the wave gauge No. 2 [H3]. The wave reflection energy from the beach (at the downstream end of flume) is neglected [H4]. The plunging jet impact takes place in a region of 'relatively' shallow waters [H5] and the effects of the flume bottom might be significant.

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Overall the authors believe that the errors on the wave reflection effects caused by the sloping bottom and by the beach might "balance" each other. The reasonably good agreement between the drop structure calculations and the breaking wave calculations provides an interesting comparison, suggesting some similar dissipation processes.

Conclusion

Plunging breaking waves are an important mechanism of entrainment of air bubbles in the ocean and induce the large amount of energy dissipation. New experiments were performed in a laboratory wave flume to investigate the characteristics of the plunging jet. The main results of the study indicate that the location of the plunging jet impact with the free-surface is always above the still water level with some substantial scatter, and that the impact angle of the plunging jet with the free-surface is about 31 degrees. The rate of energy dissipation at each plunging breaker is about 20% to 60%. Energy dissipation calculations suggest that the rate of energy dissipation increases with the bubble penetration depth and with the characteristic length of the plunging jet shear flow. Interestingly the rate of energy dissipation is similar to the rate of energy dissipation at drop structures.

The writers wish to emphasise that the calculations of energy dissipation are based upon several approximations. In their opinion, the close agreement between energy dissipation calculations at plunging breakers and at drop structures confirms the soundness of the calculations.

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Notation

A	wave amplitude (m);
A _b	wave crest elevation (m) at breaking measured from the still water level;
A _i	height (m) of the plunging jet impact measured above the still water level;
A ₀	wave amplitude (m) of incoming waves;
C ₀	celerity (m/s) of incoming waves;
(D _p) _{max}	maximum air bubble penetration height (m) measured vertically from the jet impact position : $(D_p)_{\max} = (L_p)_{\max} + A_i$;
E	1- energy of the incident wave; 2- total head (m) of a free-surface flow;
g	gravity acceleration (m/s ²) : g = 9.79 m/s ² in Taiwan;
H	wave height (m) measured from crest to trough;
H _I	incident wave height (m);
H _b	breaking wave height (m) measured from crest to trough;
H ₀	1- wave height (m) of deep-water waves; 2- wave height (m) of incoming waves measured at wave gauge No. 2 (see fig. 2);

H_r	wave reflection height (m);
H_t	wave transmission height (m);
h	still water depth (m) at breaking point;
h_c	critical flow depth (m) in open channel flow;
h_o	still water level (m) measured perpendicular to the channel bottom;
K_r	wave reflection coefficient : $K_r = H_r/H_I$;
K_t	wave transmission coefficient : $K_t = H_t/H_I$;
L_o	wave length (m) of incoming waves;
$(L_p)_{\max}$	maximum penetration height (m) measured from the still water level and positive downwards;
T	wave period (s);
V	velocity (m/s);
V_b	velocity (m/s) of the wave crest at breaking point;
V_i	impact velocity (m/s) of the plunging jet,
W	channel width (m);
x	distance along the channel bottom (m);
y	distance measured perpendicular to the channel bed surface (m);
z	transverse distance (m) measured perpendicular from the right sidewall;
α	angle between the free-surface and the horizontal at impact of the plunging jet;
ΔE	1- energy dissipation by breaking wave; 2- head loss (m);
Δz	1- backward facing step height (m); 2- drop (m) at a drop structure;
θ	angle between the impinging plunging jet and the water free-surface;
ρ_w	water density (kg/m^3);

Subscript

b	flow conditions at breaking;
BEM	BEM model computations;
i	impact flow conditions at the impingement of the plunging jet with the water free-surface;
o	incoming wave flow conditions;
r	wave reflection;
t	wave transmission;

Abbreviations

BEM	Boundary Element Method.
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Appendix A - Energy dissipation calculations

The energy dissipation by plunging breaking waves downstream of the sloping bottom was estimated by comparing the wave height measurements at wave gauges No. 2 and 3 (see fig. 2) with ideal-fluid flow computations.

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The ideal-fluid flow computations were performed with a Boundary Element Method (BEM) model. The BEM model was a simplification of the two-dimensional steady flow model developed by LEE (1995). The incident wave flow conditions (see below) were set at the upstream boundary. The computations provided the (ideal-flow) wave transmission over the sloping bottom and the wave reflection. The rate of energy dissipation by plunging breaking waves was deduced from the difference of the wave transmission energy for ideal fluid flow (BEM model) minus the measured wave transmission energy (data). It yields :

$$\frac{\Delta E}{E} = \left(\frac{(H_t)_{BEM}}{H_o} \right)^2 - \left(\frac{(H_t)_{data}}{H_o} \right)^2 = ((K_t)_{BEM})^2 - ((K_t)_{data})^2 \quad (A1)$$

During the experiments, the incident flow properties (at the wave maker) were not available. Computations showed that wave reflection coefficient was not zero, implying that the measured wave height H_o was in fact the superposition of the incident wave height H_I and the reflected wave height H_r at that location.

Run No.	Wave No.	Wave celerity C ₀ data m/s	Wave amplitude A ₀ data m	Wave period T data s	Wave height H ₀ data G2 m	Transmit. wave height H _t data G3 m	Reflected wave height H _r BEM (a) m	Transmit. wave height H _t BEM (b) m	Wave reflection coeff. K _r BEM	Wave transmis. coeff. K _t BEM	Rate of energy dissipat. ΔE/E (c) %	Rate of energy dissipat. ΔE/E (d) %
(1)	(2)	(3)	(4)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
Series 1												
1A	3	1.3595	0.0349	1.256	0.0617	0.0465	0.0149	0.0598	0.243	0.969	37.1	46.3
	4	1.3019	0.0463	1.163	0.071	0.0551	0.0172	0.0687	0.243	0.969	33.6	--
	5	1.2804	0.0457	1.092	0.0696	0.0475	0.0161	0.0675	0.233	0.971	47.8	50.1
	6	1.2407	0.0459	1.073	0.0768	0.0462	0.0175	0.0746	0.229	0.972	58.3	--
1B	3	1.2864	0.0347	1.258	0.0615	0.0471	0.0147	0.0596	0.241	0.970	35.4	47.3
	4	1.3269	0.0469	1.167	0.0706	0.0613	0.0171	0.0683	0.244	0.969	18.5	46.7
	5	1.2962	0.0467	1.094	0.0708	0.0521	0.0165	0.0687	0.234	0.971	40.1	48.7
1C	3	1.3605	0.0293	1.270	0.0546	0.0449	0.013	0.0529	0.239	0.970	26.6	--
	4	1.3274	0.0444	1.203	0.0689	0.051	0.0168	0.0667	0.244	0.969	39.1	50.1
	5	1.3	0.0454	1.082	0.0696	0.0518	0.016	0.0675	0.231	0.972	39.0	49.7
1D	3	1.3081	0.035	1.251	0.0622	0.0464	0.015	0.0603	0.241	0.970	38.4	47.6
	4	1.2978	0.0466	1.164	0.0708	0.0585	0.0172	0.0685	0.244	0.969	25.6	--
	5	1.2993	0.0465	1.088	0.0712	0.0523	0.0164	0.0691	0.232	0.971	40.4	50.7
1E	3	1.3079	0.0348	1.256	0.0615	0.0476	0.0148	0.0596	0.241	0.970	34.2	--
	4	1.3204	0.0455	1.172	0.0696	0.0559	0.0169	0.0674	0.244	0.969	29.4	--
	5	1.2967	0.0453	1.090	0.0685	0.0534	0.0159	0.0664	0.233	0.971	33.4	--
	6	1.28	0.0447	1.072	0.0755	0.0495	0.0172	0.0733	0.228	0.972	51.5	--
1F	4	1.2961	0.044	1.219	0.0693	0.0491	0.0168	0.0671	0.243	0.969	43.8	--
	5	1.3018	0.0457	1.099	0.0694	0.051	0.0162	0.0673	0.234	0.970	40.1	--
	6	1.2685	0.0458	1.080	0.0724	0.0514	0.0166	0.0703	0.230	0.972	44.0	--
1G	3	1.2775	0.0342	1.258	0.0608	0.0472	0.0146	0.0589	0.241	0.970	33.9	--
	4	1.2947	0.0458	1.190	0.0695	0.0532	0.0169	0.0673	0.244	0.969	35.3	--
	5	1.2846	0.0455	1.094	0.069	0.0497	0.016	0.0669	0.233	0.971	42.4	--
1H	4	1.4652	0.0407	1.150	0.0706	0.052	0.0171	0.0683	0.242	0.969	39.7	--
	5	1.3959	0.0473	1.110	0.0694	0.0496	0.0164	0.0672	0.234	0.970	43.0	--
Series 2												
2A	3	1.388	0.0413	1.110	0.0722	0.0577	0.0146	0.0705	0.203	0.978	31.8	--
	4	1.284	0.0504	1.060	0.0799	0.0666	0.0156	0.0781	0.197	0.979	26.3	--
	5	1.2662	0.0499	1.009	0.0806	0.0499	0.0149	0.079	0.186	0.983	58.3	--
2B	3	1.3261	0.0407	1.151	0.0702	0.057	0.0142	0.0686	0.203	0.978	29.7	--
	4	1.2934	0.0503	1.053	0.081	0.0689	0.0158	0.0792	0.195	0.980	23.5	--
	5	1.3363	0.0492	1.011	0.0802	0.0554	0.0149	0.0786	0.187	0.983	48.8	--
2C	3	1.3302	0.0407	1.148	0.0701	0.0587	0.0142	0.0685	0.203	0.978	25.6	--
	4	1.2882	0.0492	1.057	0.0806	0.0691	0.0157	0.0788	0.196	0.979	22.5	--
	5	1.2622	0.0488	1.013	0.0804	0.0634	0.0149	0.0788	0.187	0.982	34.4	47.9
2D	3	1.2951	0.0395	1.157	0.069	0.0571	0.0139	0.0674	0.203	0.978	27.1	--
	4	1.3047	0.0503	1.060	0.0817	0.0669	0.016	0.0799	0.197	0.979	28.8	--
	5	1.3373	0.0486	1.018	0.0797	0.0588	0.0149	0.0781	0.188	0.982	42.0	47.9
	7	1.35	0.0604	0.959	0.0929	0.0623	0.0164	0.0913	0.178	0.986	52.1	48.7
2E	3	1.3396	0.0409	1.150	0.07	0.0574	0.0142	0.0684	0.203	0.978	28.4	40.5
	4	1.2995	0.0523	1.053	0.0814	0.066	0.0158	0.0796	0.195	0.980	30.2	46.5
2F	3	1.3026	0.0483	1.115	0.0782	0.0634	0.0158	0.0764	0.203	0.978	29.8	--
	4	1.2892	0.0482	1.028	0.0777	0.0602	0.0147	0.0761	0.190	0.981	36.2	--
	5	1.3015	0.0496	0.993	0.0813	0.0548	0.0148	0.0798	0.183	0.984	51.4	--
2G	3	1.352	0.0407	1.152	0.0706	0.0602	0.0143	0.069	0.203	0.978	22.9	--
	4	1.3034	0.0511	1.049	0.0819	0.0698	0.0159	0.0801	0.195	0.980	23.4	--
	5	1.2584	0.0496	1.016	0.0848	0.0535	0.0158	0.0831	0.188	0.982	56.7	--
2H	4	1.2946	0.0492	1.081	0.0802	0.0634	0.016	0.0783	0.200	0.978	33.3	--
2I	3	1.3136	0.0408	1.149	0.0697	0.0596	0.0141	0.0681	0.203	0.978	22.6	--
	4	1.2792	0.0502	1.054	0.0805	0.0678	0.0157	0.0787	0.195	0.980	25.0	--

Run No.	Wave No.	Wave celerity C_o data m/s	Wave amplitude A_o data m	Wave period T data s	Wave height H_o data G2 m	Transmit. wave height H_t data G3 m	Reflected wave height H_r BEM (a) m	Transmit. wave height H_t BEM (b) m	Wave reflection coeff. K_r BEM	Wave transmis. coeff. K_t BEM	Rate of energy dissipat. $\Delta E/E$ (c) %	Rate of energy dissipat. $\Delta E/E$ (d) %
(1)	(2)	(3)	(4)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
Series 3												
3A	3	1.2448	0.0267	1.354	0.0535	0.036	0.0149	0.0513	0.279	0.959	46.8	50.2
	4	1.3146	0.0334	1.305	0.0598	0.0379	0.017	0.0572	0.284	0.958	51.6	48.8
	5	1.2903	0.0361	1.229	0.0604	0.0406	0.0173	0.0578	0.287	0.957	46.4	49.5
	6	1.2714	0.0369	1.196	0.0583	0.0374	0.0166	0.0558	0.285	0.958	50.5	49.3
3B	3	1.2636	0.0302	1.341	0.0544	0.0373	0.0152	0.0521	0.281	0.959	44.9	48.6
	4	1.2916	0.0378	1.274	0.0617	0.0366	0.0176	0.059	0.287	0.957	53.0	48.3
	5	1.2873	0.0378	1.193	0.0588	0.0388	0.0167	0.0563	0.285	0.958	48.1	50.9
3C	3	1.2548	0.0284	1.362	0.0527	0.0386	0.0146	0.0505	0.277	0.960	38.5	49.1
	4	1.2622	0.0339	1.326	0.0593	0.0424	0.0167	0.0586	0.282	0.959	40.8	--
3D	3	1.2357	0.0288	1.342	0.0545	0.0319	0.0153	0.0522	0.281	0.959	57.8	49.9
	4	1.2933	0.0371	1.273	0.0608	0.0364	0.0174	0.0582	0.287	0.957	55.8	50.8
3E	3	1.2239	0.0288	1.340	0.0545	0.0343	0.0152	0.0522	0.281	0.959	52.4	--
3F	3	1.2505	0.029	1.338	0.0548	0.0353	0.0154	0.0525	0.281	0.959	50.5	--
	4	1.23	0.038	1.276	0.0622	0.0381	0.0148	0.0595	0.287	0.958	54.2	--
3G	3	1.2468	0.0283	1.347	0.0541	0.0349	0.0151	0.0519	0.280	0.959	50.4	--
	4	1.3069	0.0371	1.277	0.0612	0.0372	0.0175	0.0586	0.287	0.958	54.7	--
3H	3	1.2959	0.0273	1.335	0.055	0.0347	0.0154	0.0527	0.281	0.959	52.1	--
	4	1.2952	0.0366	1.274	0.062	0.0371	0.0177	0.0593	0.287	0.957	55.9	--

Comments :

BEM : BEM model calculations

Data : experimental data

Data G2 : experimental data recorded at gauge No. 2

Data G3 : experimental data recorded at gauge No. 3

$\Delta E/E$: rate of energy dissipation

(a) : wave reflection height at the upstream open boundary located 4 wave depths upstream of the sloping bottom

(b) : wave transmission height at the wave gauge No. 3

(c) : wave energy dissipation (column 13)

(d) : drop structure energy dissipation calculated using equations (5) and (6) with $h_c = 0.1 * H_b$ and $\Delta z = A_b - A_i$ (column 14)

Table 1 - Experimental flow conditions

Run	Flow depth h_o m	Wave celerity C_o m/s	Wave amplitude A_o m	Wave length L_o m
(1)	(2)	(3)	(4)	(5)
Series 1	0.1995	1.14 to 1.34	0.029 to 0.047	1.33 to 1.73
Series 2	0.2172	1.26 to 1.35	0.0395 to 0.052	1.28 to 1.56
Series 3	0.18525	1.246 to 1.35	0.027 to 0.038	1.52 to 1.73

Note : experimental flow conditions corresponding to the third to seventh waves.

Table 2 - Breaking velocity results

Ref.	Flow depth h _o m	Wave celerity C _o m/s	V _b /C _o Mean value	V _b /C _o Standard deviation	Nb of Exp.	Comments
(1)	(2)	(3)	(4)	(5)	(6)	(7)
Present study						
Series 1	0.1995	1.14 to 1.33	1.12	0.260	13	Backward-facing step : Δz = 0.1312 m.
Series 2	0.2172	1.26 to 1.35	1.03	0.097	19	
Series 3	0.18525	1.25 to 1.35	0.96	0.092	11	
Experiments						
IVERSEN (1951)	0.701	1.4 to 3.9	0.492	0.171	5	Beach slope : 1:10.
	0.45	2.4 to 3	0.338	N/A	2	Beach slope : 1:20
CHAN (1994)	0.60	1.70	1.24		1	Impact on vertical structure (fig. 4).
CHAN and MELVILLE (1988)	0.60	1.44	1.37		1	In absence of structure (fig. 2).
Calculations						
BIESEL (1951)			0.36	N/A	1	Calculation (1st-order theory).
			0.55	N/A	1	Calculation (2nd-order theory).

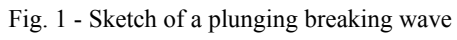


Fig. 2 - Sketch of the experimental setup

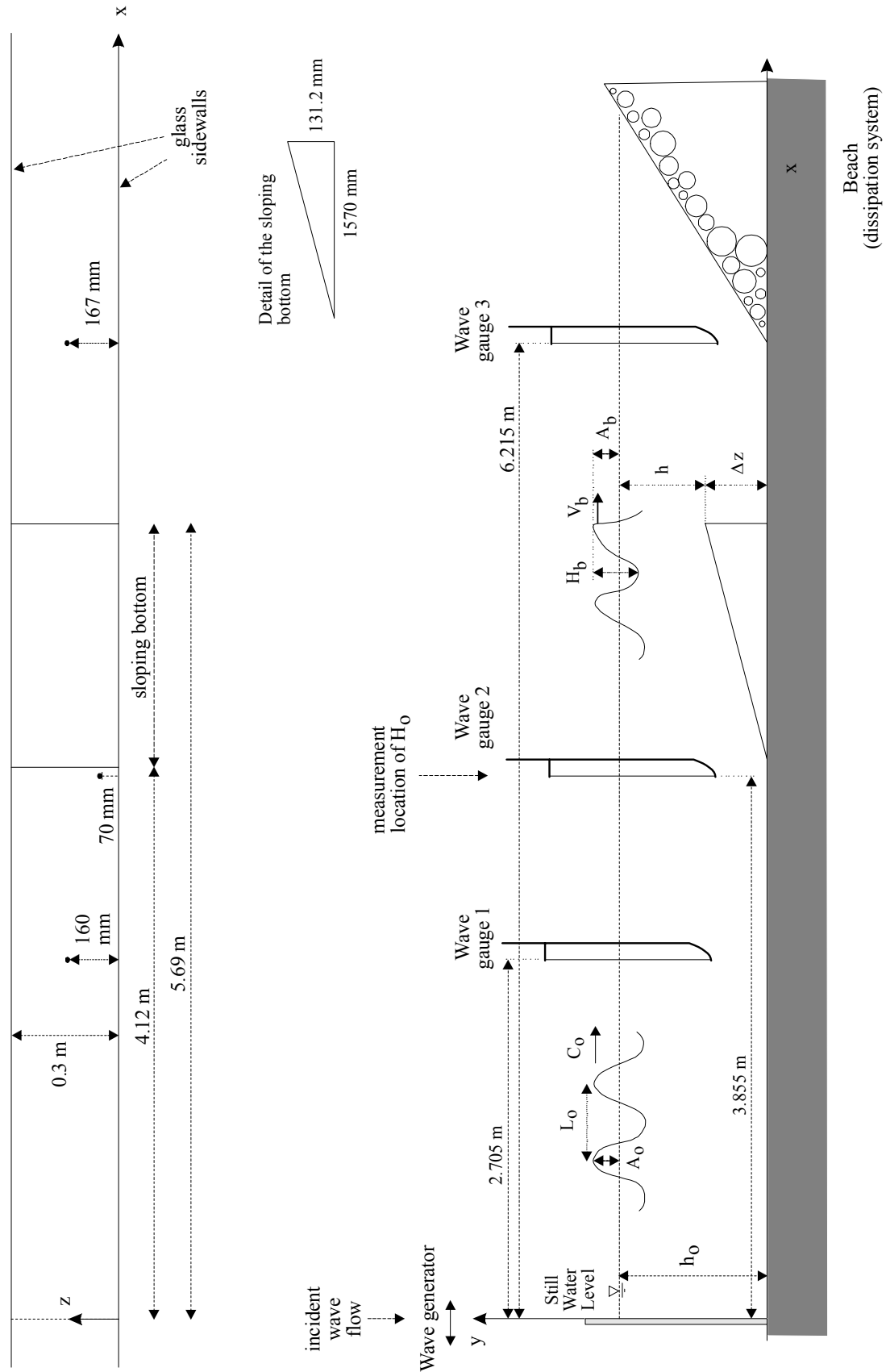


Fig. 3 - Wave breaking parameters

(A) Wave breaking height $H_b/(g \cdot T^2)$ as a function $h/(g \cdot T^2)$ - Comparison between experimental data and the results of IPPEN (1966)

(B) Wave breaking velocity V_b/C_0 as a function of A_b/d

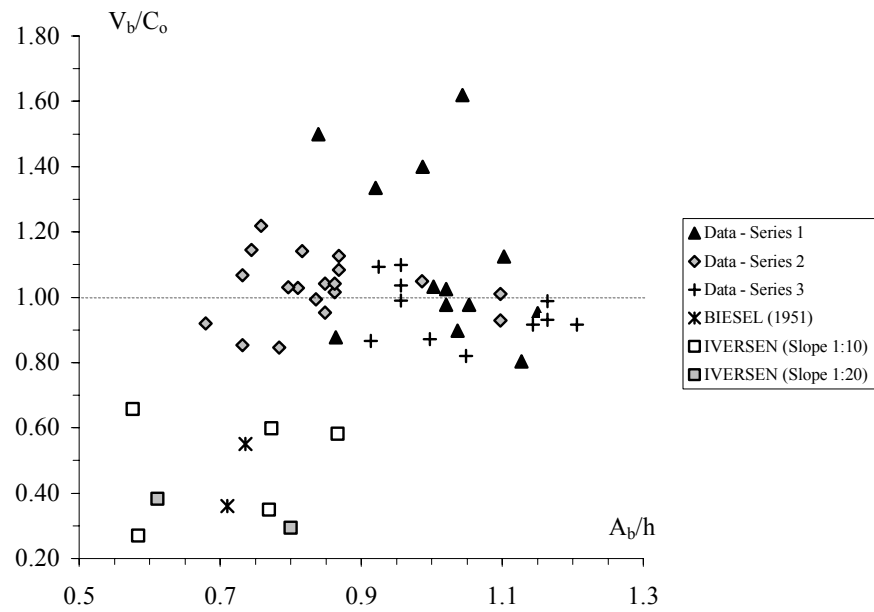
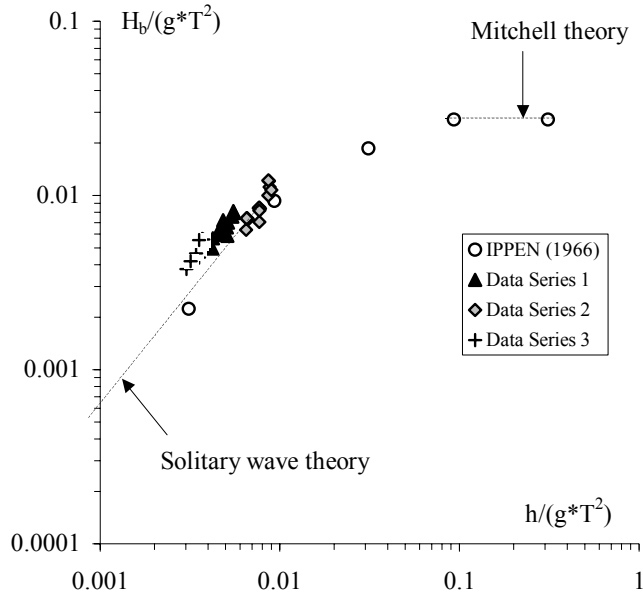


Fig. 4 - Jet impact height above still water level A_i/A_b as a function of the ratio A_o/L_o

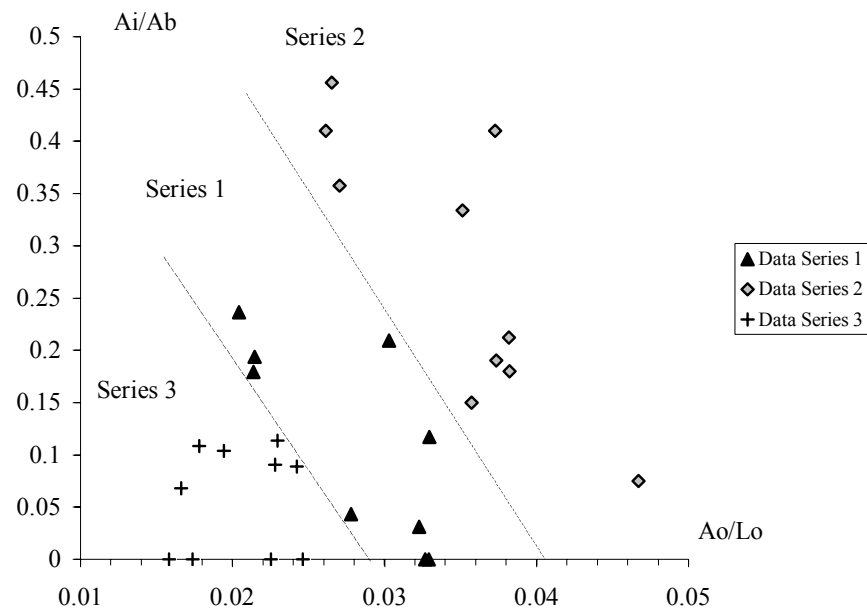


Fig. 5 - Plunging jet impact parameters

(A) Plunging jet angle θ with the free-surface as a function of the ratio A_0/L_0

(B) Free-surface slope α at the jet impact as a function of the ratio A_0/L_0

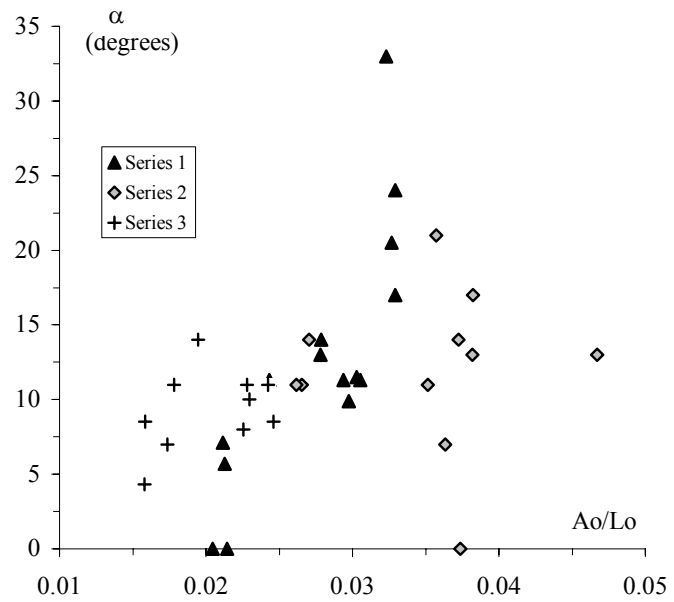
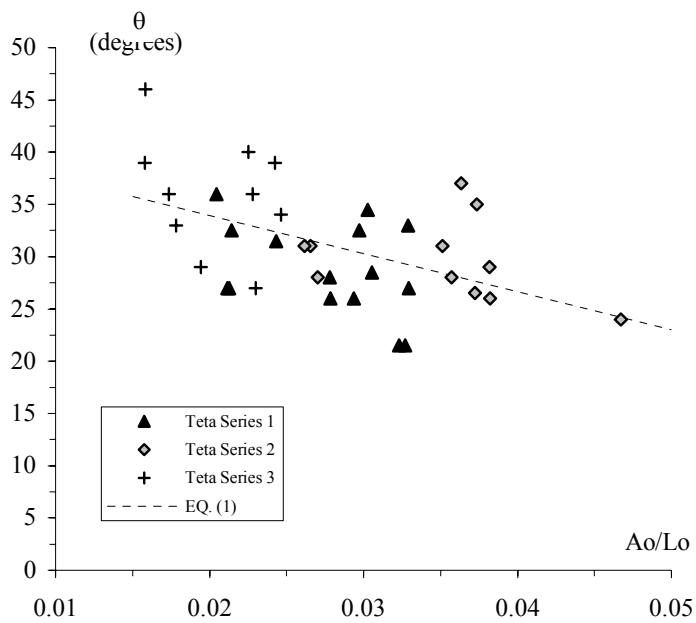


Fig. 6 - Jet impact angle : comparison between equation (3) and experimental data

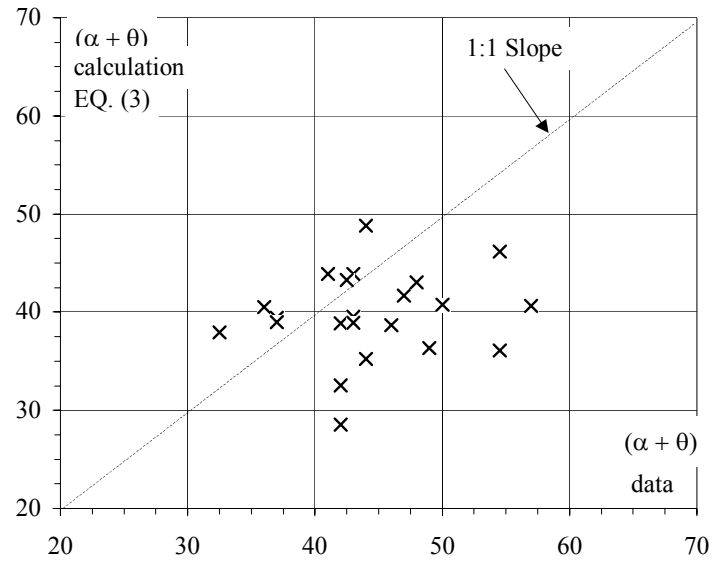


Fig. 7 - Maximum bubble penetration depth $(D_p)_{\max}/A_0$ as a function of the ratio A_0/L_0

Note : $(D_p)_{\max}$ is the penetration depth measured vertically from the impingement point

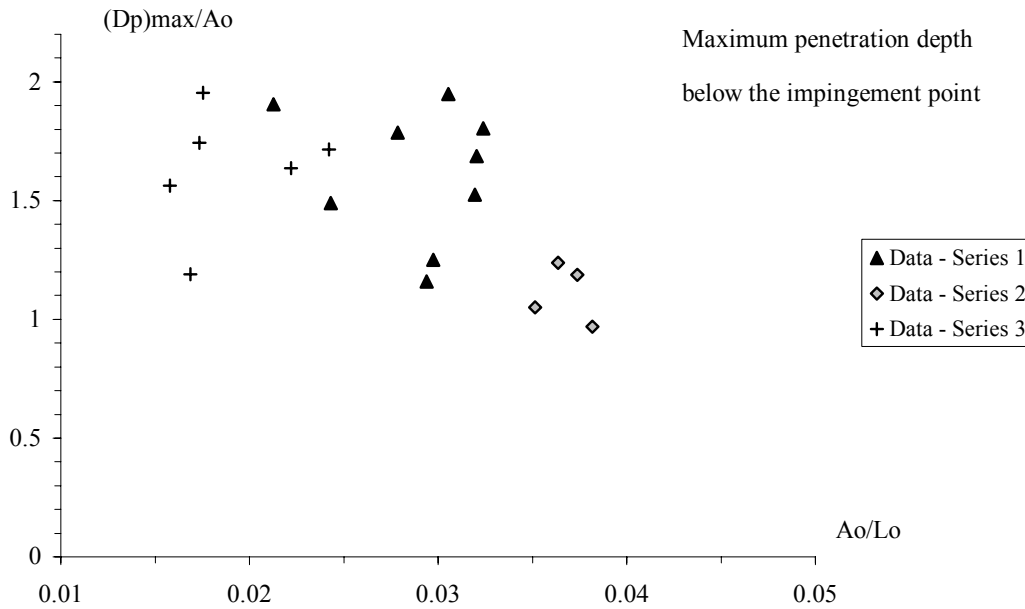


Fig. 8 - Rate of energy dissipation by plunging breaking wave

(A) $\Delta E/E$ as a function of the wave steepness A_0/L_0

(B) $\Delta E/E$ as a function of the dimensionless penetration depth $(D_p)_{\max}/A_0$

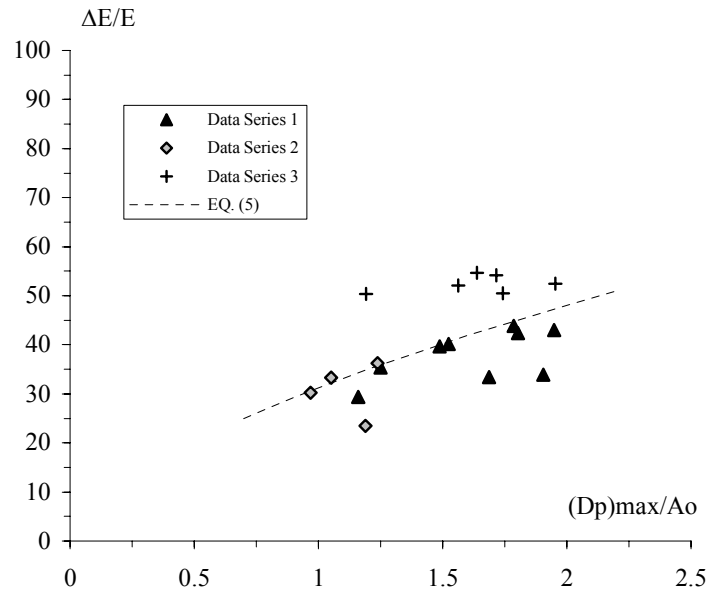
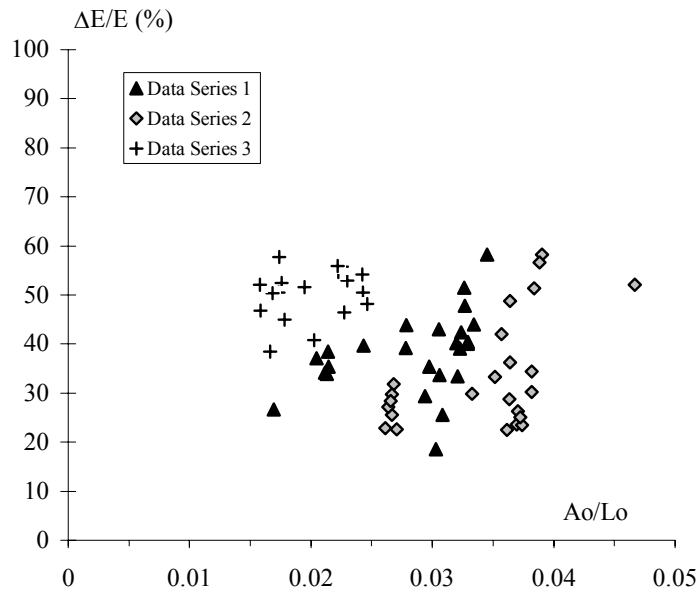


Fig. 9 - Comparison of energy dissipation at drop structures and at plunging breaking waves

(A) Sketch of a drop structure (after CHANSON 1995a)

(B) Comparison of energy dissipation at drop structures (vertical axis) with that at plunging breaking waves (horizontal axis) for similar flow conditions - Calculations performed assuming a plunging jet thickness of $0.1 \cdot H_b$

